

# Bram's Odyssey



Barry Koren

San Diego, June 22-23, 2013

# Minimax problem

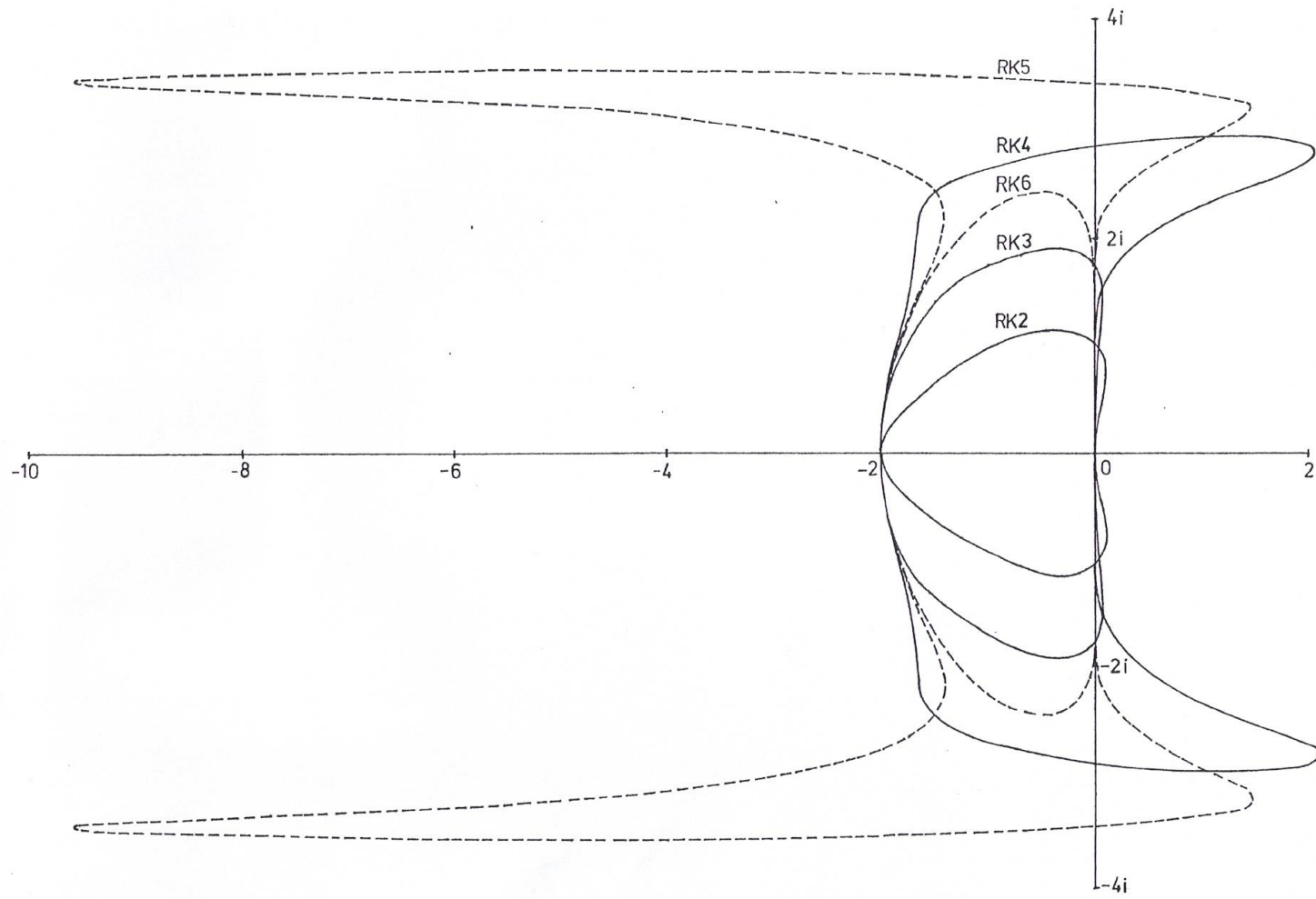


fig.2.2: Neutral stability curves Runge-Kutta schemes

# Minimax problem

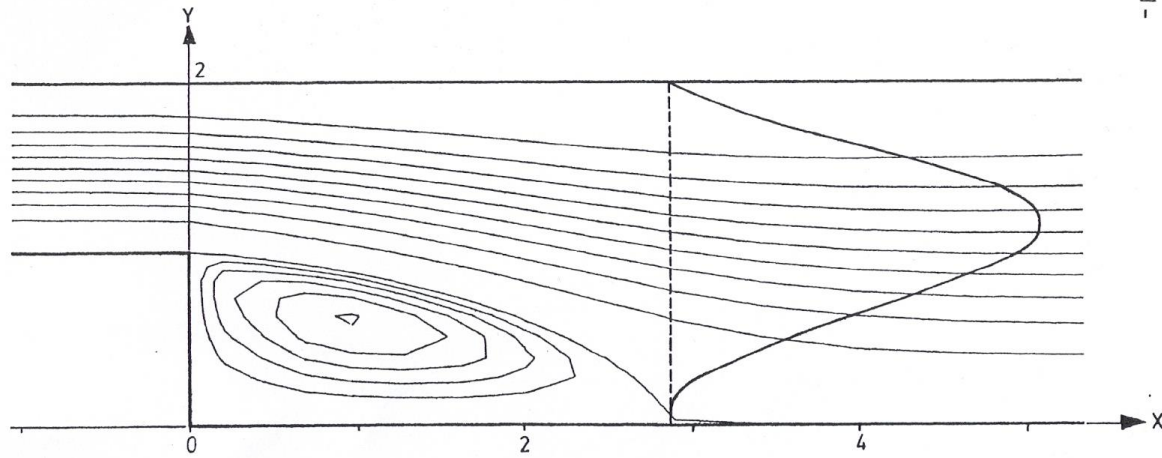
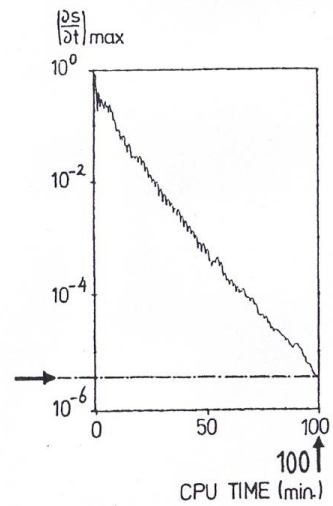
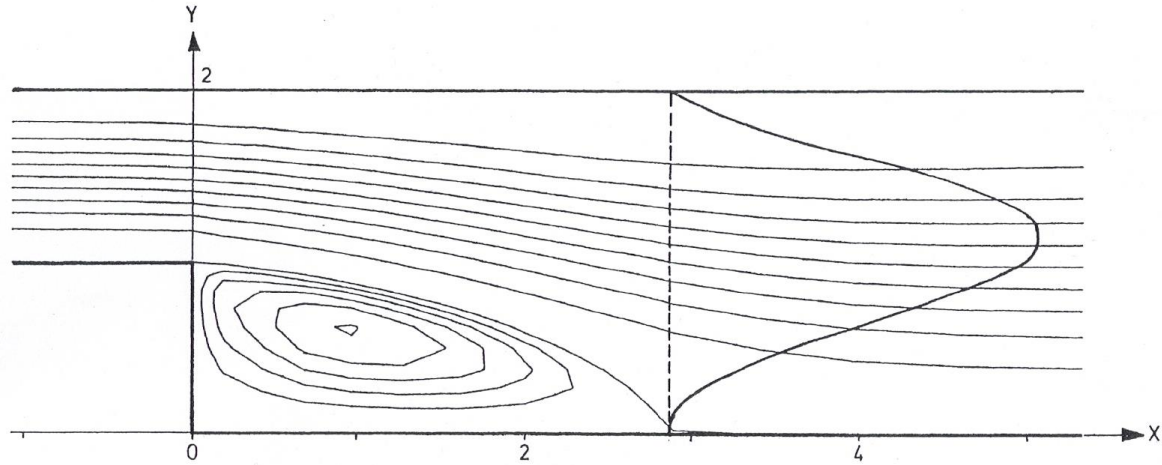
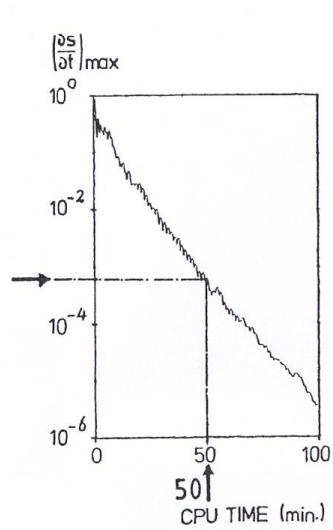


fig.3.4d: Streamline distribution after 50 and 100 minutes CPU TIME; channel with small inlet,  $Re=50$

# Minimax problem



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REPORT 84-25

A minimax problem  
along the imaginary axis

by

P. Sonneveld and B. van Leer

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Rapporten van de  
Onderafdeling der Wiskunde  
en Informatica

Reports of the  
Department of Mathematics  
and Informatics

# Start Odysseey



# Van de Hulst & Oort



# Bram & Lia, 1966



# PhD-thesis, 1970

a choice  
of  
difference schemes  
for  
ideal compressible flow



bram van leer



# Towards V, 1979

Bram van Leer

JOURNAL OF COMPUTATIONAL PHYSICS **135**, 229–248 (1997)  
ARTICLE NO. CP975704

## Towards the Ultimate Conservative Difference Scheme V. A Second-Order Sequel to Godunov's Method

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Received October 18, 1977; revised October 17, 1978

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A method of second-order accuracy is described for integrating the equations of ideal compressible flow. The method is based on the integral conservation laws and is dissipative, so that it can be used across shocks. The heart of the method is a one-dimensional Lagrangean scheme that may be regarded as a second-order sequel to Godunov's method. The second-order accuracy is achieved by taking the distributions of the state quantities inside a gas slab to be linear, rather than uniform as in Godunov's method. The Lagrangean results are remapped with least-squares accuracy onto the desired Euler grid in a separate step. Several monotonicity algorithms are applied to ensure positivity, monotonicity, and nonlinear stability. Higher dimensions are covered through time splitting. Numerical results for one-dimensional and two-dimensional flows are presented, demonstrating the efficiency of the method. The paper concludes with a summary of the results of the whole series "Towards the Ultimate Conservative Difference Scheme." © 1979 Academic Press

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### 1. INTRODUCTION

This paper describes a method of second-order accuracy

tions, with due care taken to account for the discontinuities in the interaction flow. The convective difference scheme, hidden in the Lagrangean scheme, for integrating the characteristic equations is a so-called up-stream-centered (upwind) scheme and has been discussed as "scheme II" in the previous paper [2] of this series. Remapping the Lagrangean results onto an Euler grid is done according to the upstream-centered "scheme III" from the same paper. A substantial improvement will still result if, in the Lagrangean step, scheme II is replaced by the more accurate scheme III.

An accessory technique for preserving monotonicity during convection, also discussed in [2], is easily incorporated in the method. It is applied in its crudest form [2, Eq. (66)] at the beginning of the Lagrangean step; a more sophisticated form [2, Eq. (74)] is applied in the remap step. Further refinement of the technique has been projected.

Numerical experiments indicate that for solving two-dimensional flow problems, even on a coarse grid, the present second-order method is at least an order of magni-

# Van Leer FVS, 1982

## FLUX-VECTOR SPLITTING FOR THE EULER EQUATIONS

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### Introduction

When approximating a hyperbolic system of conservation laws  $w_t + \{f(w)\}_x = 0$  with so-called upwind differences, we must, in the first place, establish which way the wind blows. More precisely, we must determine in which direction each of a variety of signals moves through the computational grid. For this purpose, a physical model of the interaction between computational cells is needed; at present two such models are in use.

In one model, neighboring cells interact through discrete, finite-amplitude waves. The nature, propagation speed and amplitude of these waves are found by solving, exactly or approximately, Riemann's initial-value problem for the discontinuity at the cell interface. We may call this the Riemann approach (Fig. 1a). The numerical technique of distinguishing between the influence of the forward- and the backward-moving waves is called flux-difference splitting; examples are the methods of Roe [1] and of Osher [2].

In the other model, the interaction of neighboring cells is accomplished through mixing of pseudo-particles that move in and out of each cell according to a given velocity distribution. We may call this the Boltzmann approach (Fig. 1b). The numerical technique of distinguishing between the influence of the forward- and the backward-moving particles is called flux-vector splitting or simply flux-splitting; an example is the "beam scheme" of Prendergast [3], rediscovered by Steger and Warming [4].

Both kinds of splitting are discussed by Harten, Lax and Van Leer [5].

The present paper is restricted to flux-vector splitting for the Euler equations of compressible flow, with the ideal-gas law used as equation of state.

# Van Leer FVS, 1990

*Barry Koun*

## Flux Vector Splitting for the 1990's

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February 1990

College of Engineering

**DEPARTMENT OF AEROSPACE ENGINEERING**

The University of Michigan  
Ann Arbor, Michigan 48109-2140



# ICASE, 1984



# ICASE Report

Benny Kosen

I C A S E

Special Internal Report

Pink Grundlehrer Series #2

'A ONE-SIDED VIEW'

Note: Reports in the ICASE Grundlehrer Series have no intrinsic value, scientific or otherwise.

# Woudschoten, 1984

*Barry Kolen*

## CONFERENTIE VAN NUMERIEK WISKUNDIGEN

*15, 16 en 17 oktober 1984*

CONFERENTIEOORD WOUDSCHOTEN  
ZEIST



Werkgemeenschap Numerieke Wiskunde

# Woudschoten, 1984

- 2 -

## UITGENODIGDE SPREKERS

Thema 1. J.J. Chattot, Matra Industries, Velizy  
B. van Leer, Technische Hogeschool Delft  
H. Viviand, ONERA, Parijs

Thema 2. R. Beauwens, Vrije Universiteit Brussel  
J. Periaux, Avions Marcel Dassault, Parijs  
D.M. Young, University of Texas, Austin  
G. Golub, Stanford University (onder voorbehoud)

De Heer Chattot komt in de plaats van Temam. Op het gebied van de Euler-vergelijkingen werkt hij samen met de groep van Prof. Temam.

Tijdens de laatste fase van de voorbereidingen is gebleken dat Prof. Golub rond half oktober zal deelnemen aan een conferentie in Leuven. Dit was voor de organisatiecommissie aanleiding hem uit te nodigen ook een voordracht in Zeist te verzorgen (binnen thema 2).

A.O.H. Axelsson en H. Schippers hebben zich aangemeld voor een korte bijdrage.

# INRIA, 1986

## NOTES ON NUMERICAL FLUID MECHANICS

Volume 26

Alain Dervieux  
Bram Van Leer  
Jacques Periaux  
Arthur Rizzi (Eds.)

**Numerical Simulation  
of Compressible Euler Flows**

Vieweg



# Hermes, 1987



# Delft, 1989



# Delft, 1989



# San Diego, 1995



# Ann Arbor, 1996



# Ann Arbor, 1997



# Ann Arbor, 1997

С.К.ГОДУНОВ



## *ВОСПОМИНАНИЯ*

*О РАЗНОСТНЫХ СХЕМАХ*



# AIAA, Chicago, 2010

## HISTORY OF CFD: PART II

© 2010: Bram van Leer & Marcus Lo



Top level: Jay Boris, Vladimir Kolgan, Bram van Leer, Antony Jameson

Ground level: Richard Courant, Kurt Friedrichs, Hans Lewy, Robert MacCormack, Philip Roe, John von Neumann, Stanley Osher, Amiram Harten, Peter Lax, Sergei Godunov



# CWI, 1993-2007



# Leiden, 2012



# Leiden, 2012



# Leiden, 2012



# Leiden, 2012



# Van Leer Family, 2006



# Van Leer Family, 2008



# You're welcome!

