



**1st International Workshop on High-Order CFD Methods, Nashville, January 7-8, 2012**

## **Summary of the C2.4 test case results**

**Ralf Hartmann**

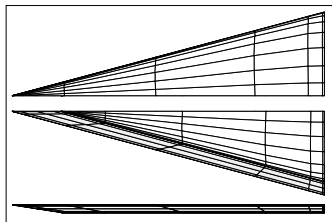
Institute of Aerodynamics and Flow Technology  
German Aerospace Center

8. Jan. 2012

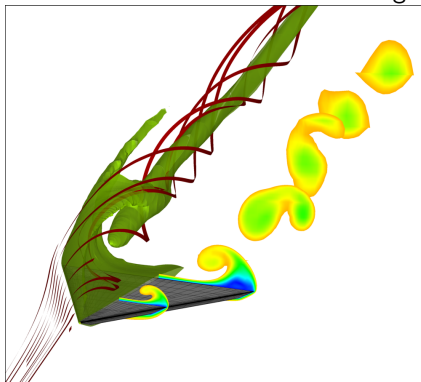


## Test case C2.4

Laminar flow at  $M = 0.3$ ,  $Re = 4000$  and  $\alpha = 12.5^\circ$  around the delta wing



geometry



Mach number isosurfaces (left) and slices (right) [LH10]

Reference values

(taken from [LH10]):

$$C_d^{\text{ref}} = 0.1658, C_l^{\text{ref}} = 0.347.$$

[LH10] T. Leicht and R. Hartmann. Error estimation and anisotropic mesh refinement for 3d laminar aerodynamic flow simulations. J. Comput. Phys., 229(19), 7344-7360, 2010.

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**Following nested hexahedral meshes have been provided on the workshop (hiocfd) homepage**

- ▶ delta.1.msh with 408 cells
- ▶ delta.2.msh with 3,264 cells
- ▶ delta.3.msh with 26,112 cells
- ▶ delta.4.msh with 208,896 cells

**“Official” convergence criterion (taken from “Notes for all participants”)**

Reduction of the density residual to  $10^{-10}$  relative to freestream conditions measured in a normalized  $L^2$ -norm, i.e.

$$R/R_\infty < 10^{-10} \quad \text{for} \quad R = L^2(Res_\rho) = \sqrt{\frac{1}{N} \sum_i^N Res_{\rho,i}^2}$$

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### Data available from

- ▶ Alessandro Colombo, Francesco Bassi, University of Bergamo, **UBerg**
- ▶ Krzysztof Fidkowski, University of Michigan, **UMich**
- ▶ Ralf Hartmann, DLR, Braunschweig, **DLR**
- ▶ Li Wang, J. Taylor Erwin, W. Kyle Anderson, University of Tennessee, **UTenn**

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Laminar flow at  $M = 0.3$ ,  $Re = 4000$  and  $\alpha = 12.5^\circ$  around the delta wing

### Case details

	<b>UBerg</b>	<b>UMich</b>	<b>DLR</b>	<b>UTenn</b>
discretization	DG, BR2	DG, BR2 ?	DG, BR2	DG, SIPG
basis functions	$P_p(\kappa)$ , orth.norm.	$\sigma(Q_p(\hat{\kappa})) ?$	$\sigma(Q_p(\hat{\kappa}))$	$\sigma(P_p(\hat{\kappa})) ?$
numerical flux	exact Riemann	Roe ?	Roe+entropy fix	HLLC
farfield	characteristic	Roe + $\mathbf{u}_\infty ?$	characteristic	subsonic in/outflow
solver	bw Euler	Newton	Newton	p-MG+el.GS/GMRES
grid	grids (hiocfd)	grids (hiocfd)	grids (hiocfd)	unstruct./tretrah.
convergence criterion	official $R/R_\infty < 10^{-10}$ $\sqrt{\frac{1}{N} \sum_i Res_{\varrho,i}^2}$	other $R < 10^{-7}$ $\sum_i  Res_{\varrho,i} $	official $R/R_\infty < 10^{-10}$ $\sqrt{\frac{1}{N} \sum_i Res_{\varrho,i}^2}$	other $R < 10^{-11}$ $\sqrt{\frac{1}{N} \sum_i Res_{\varrho,i}^2} ?$
wall				adiabatic (instead of isothermal)

**Note**, that work units of UMich & UTenn are not comparable to others.



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## Case details

### UTenn

discretization	Petrov-Galerkin
farfield	subsonic in/outflow
solver	approx. Newton
grid	unstruct./tetrah.

convergence

$$R < 10^{-11}$$

criterion

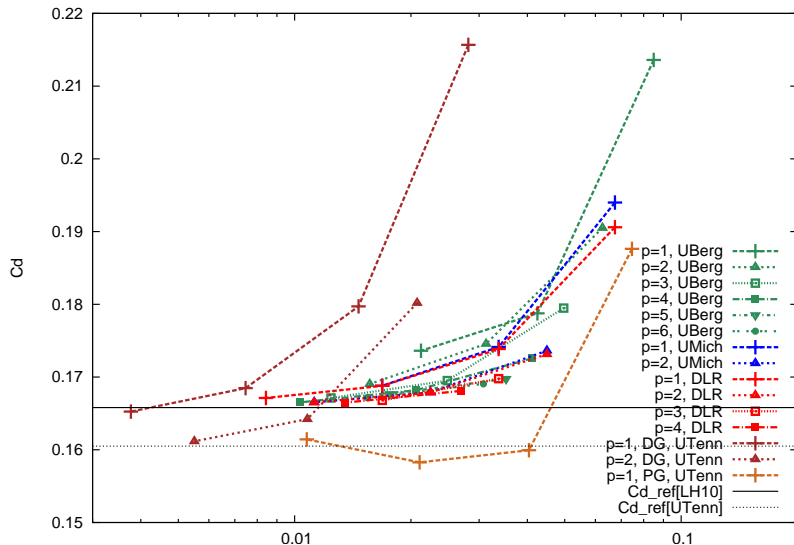
$$\sqrt{\frac{1}{N} \sum_i^N Res_{\theta,i}^2} ?$$

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## Reference values

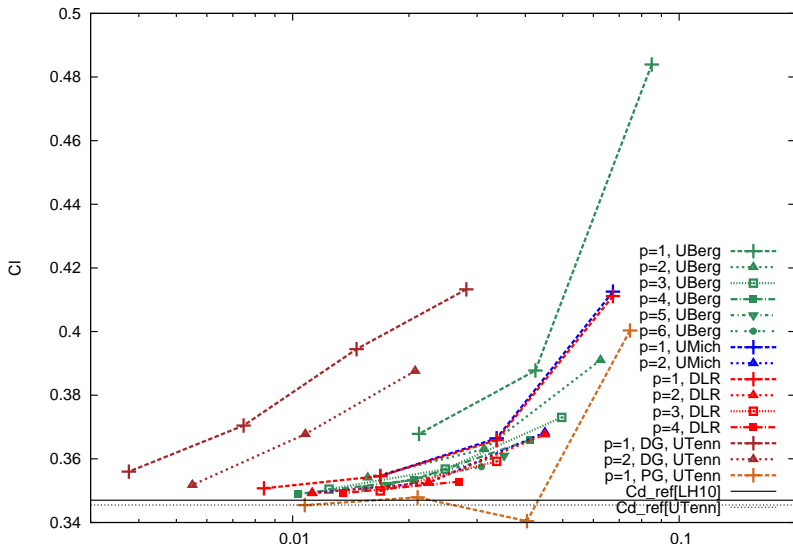
- ▶ taken from [LH10]:  $C_d^{\text{ref}} = 0.1658$ ,  $C_l^{\text{ref}} = 0.347$   
grids (hioefd), isothermal wall boundary condition
- ▶ obtained by UTenn(DG):  $C_d^{\text{ref}} = 0.1605$ ,  $C_l^{\text{ref}} = 0.3455$   
unstructured grids, adiabatic wall boundary condition

## Test case C2.4: $C_d$ vs. $h$

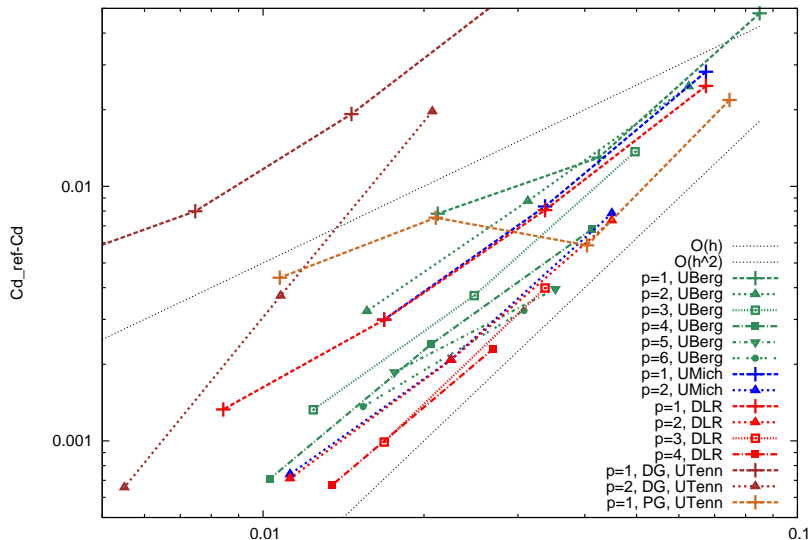




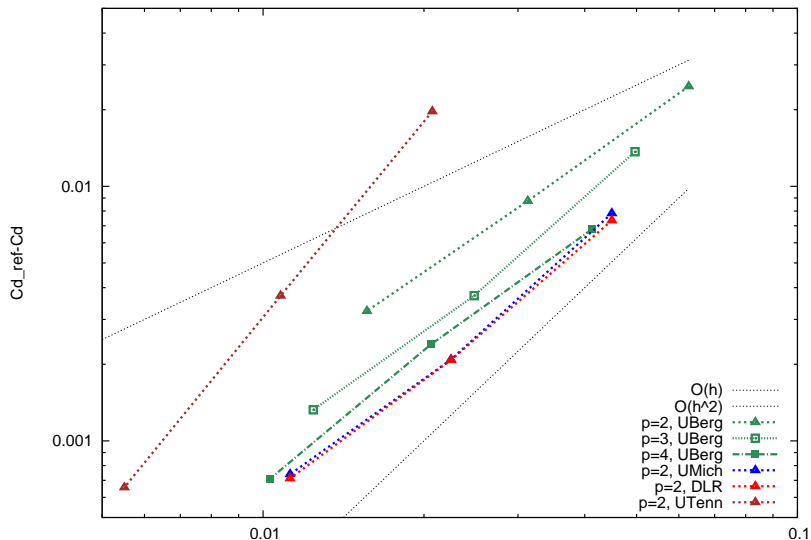
# Test case C2.4: $C_l$ vs. $h$



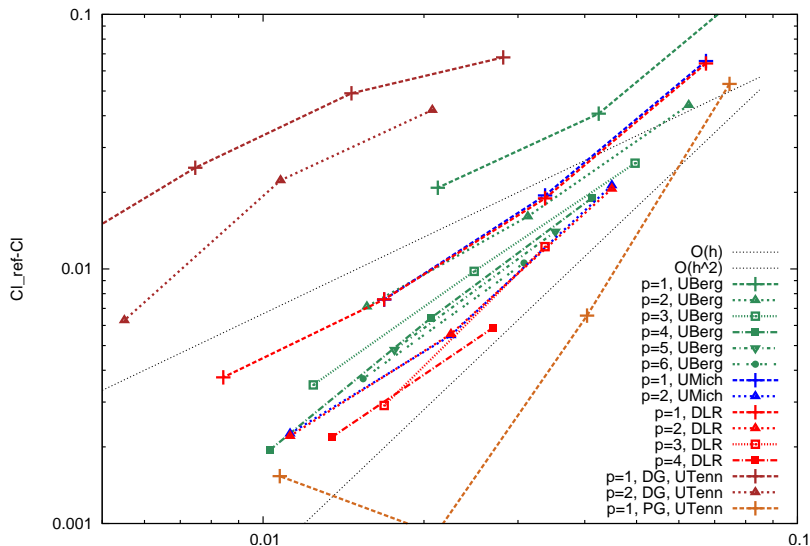
# Test case C2.4: Error in $C_d$ vs. $h$



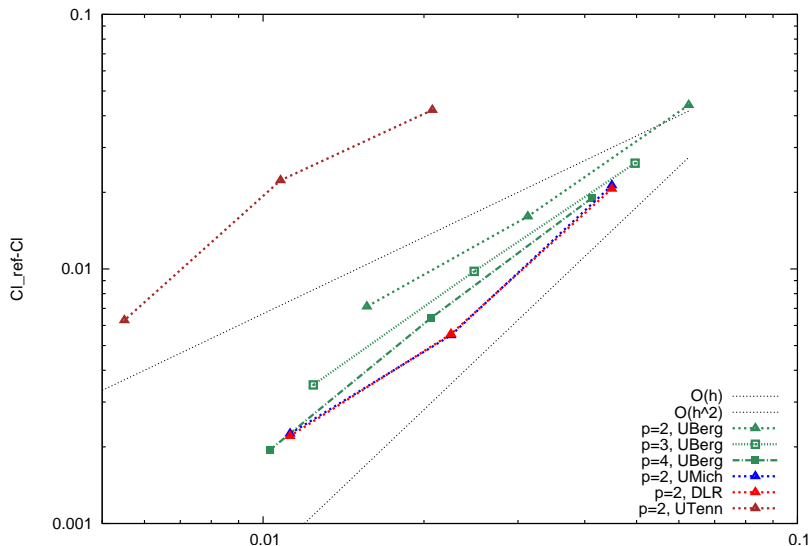
## Test case C2.4: Error in $C_d$ vs. $h$ for $p = 2$



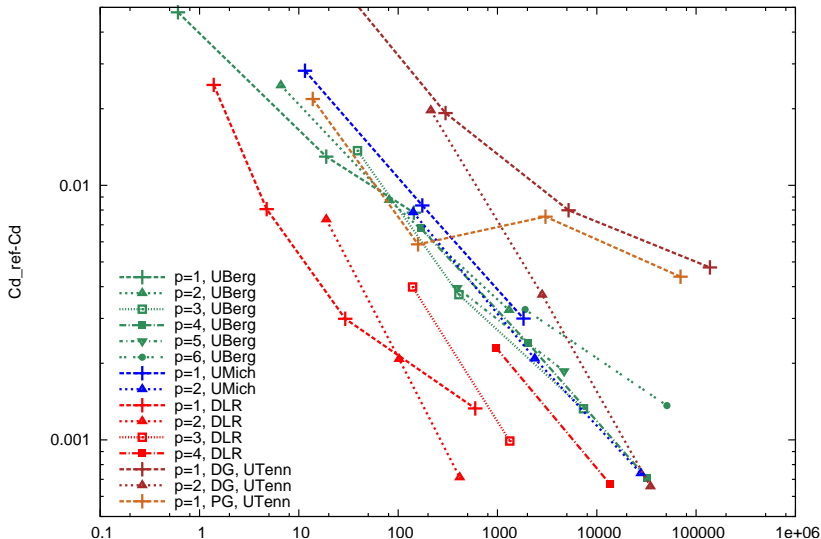
# Test case C2.4: Error in $C_l$ vs. $h$



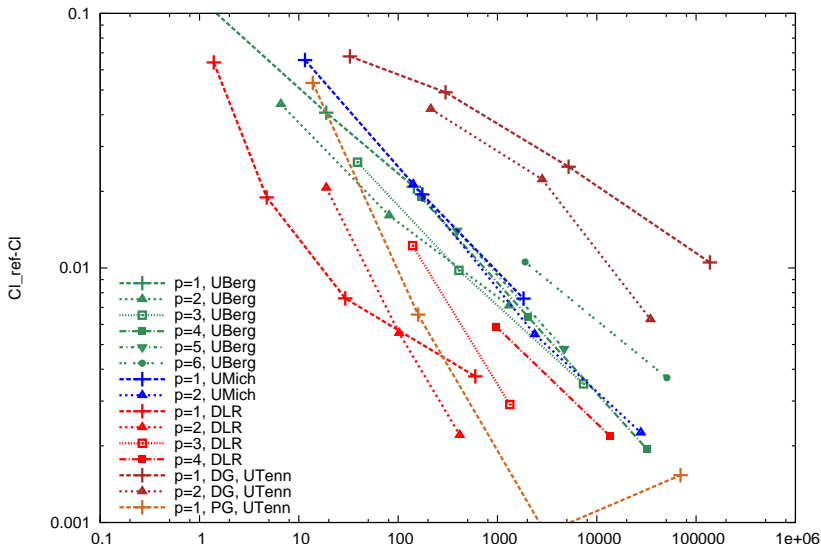
## Test case C2.4: Error in $C_l$ vs. $h$ for $p = 2$



# Test case C2.4: Error in $C_d$ vs. workunits



# Test case C2.4: Error in $C_l$ vs. workunits



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- ▶ Comparison of results of **UTenn** with the results of the other partners is difficult as **UTenn** computed on different grid sequence with different boundary conditions and different convergence criterion.





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- ▶ Very good agreement of  $C_d$  and  $C_l$  values between **UMich** and **DLR** due to the use of very similar numerical schemes.
  - ▶ However, **UMich** required a factor of 7–70 more work units than **DLR**.
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- ▶ Difference of results between **UBerg** and **UMich/DLR** due to different basis functions/discrete function spaces.
  - ▶ There is some agreement when comparing results for similar dimension of discrete function spaces instead of for the same polynomial degree.
- ▶ Due to the non-smoothness of the flow solution there is not much gain (if at all) in computing time using a global  $p$  larger than 2.